

# “Implementation of An Efficient Image Encryption-compression System using a New Haar and Coiflet with Daubchies and Symlet Wavelet Transform”

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**Abstract**—In this modern world, hidden information concept are very important and play a significant role to reducing the space in the memory as well as on disk drives. Compression of the encrypted information has taken more attention due to security reasons from last few years. If encryption and compression of the information works properly then it results to high speed computation. According to practical scenario encryption should be performed before the compression of information. Because unencrypted information have more chances of stealing. Therefore we have proposed system where encryption is done prior to the image compression by random permutation method and after that we can efficiently compress the encrypted image. In this paper, we purpose a new approach is named as ECNHCDST (Encryption-Compression using New Haar and Coiflet with Symlet and Daubchies wavelet transform). The resultant image after encryption and compression is evaluated using various parameters like CR (Compression Ratio), MSE (Mean Square Error) and PSNR (Peak signal to Noise Ratio) to check the efficiency and to compare it with the result of existing system. We also demonstrate that an arithmetic coding-based approach can be exploited to efficiently compress the encrypted images. For the implementation of this proposed work MATLAB simulator is used.

**Keywords:** Encryption, Compression, ETC, Haar, Coiflet, Symlet, Daubchies, CR, MSE, PSNR.

## 1. INTRODUCTION

The security of multimedia becomes more important, since multimedia data are transmitted over open networks more frequently. Typically, reliable security is necessary to content protection of digital images and videos [2]. Encryption and compression schemes for multimedia data need to be specifically designed to protect multimedia content and fulfill the security requirements for a particular multimedia application. Image Encryption means that convert an image to unreadable format so that it can be transmitted over the network safely. Image Decryption means to convert the unreadable format of an image to original image. This is used

to protect the secrets of corporate as well as government’s offices. [1].

**Compression:** It is done in order to save storage space or transmission time. The purpose of compression is reduction in size. The main objective behind compressing an image is to reduce the unimportant and redundant data, so as to store or transmit data in more efficient way. The applications of data compression in diverse areas are as follows:

- Satellite imagery
- Mini discs
- MP3technology
- Modems
- Digital cameras
- Database Design
- Storage and transmission of data
- Distributing Software
- Data Transmission

Image compression addresses the problem of reducing the amount of data required to represent a digital image. It is a process intended to yield a compact representation of an image, thereby reducing the image storage/ transmission requirements [3]. Compression is achieved by the removal of one or more of the three basic data redundancies:

- Coding Redundancy
- Interpixel Redundancy
- Psychovisual Redundancy

The image compression techniques are broadly classified into two categories depending whether or not an exact replica of the original image could be reconstructed using the compressed image.

These are:

- Lossless technique
- Lossy technique

### Lossless compression technique

In lossless compression techniques, the original image can be perfectly recovered from the compressed (encoded) image. These are also called noiseless since they do not add noise to the signal (image). It is also known as entropy coding since it use statistics/decomposition techniques to eliminate/ minimize redundancy. Lossless compression is used only for a few applications with stringent requirements such as medical imaging.

### Lossy compression technique

Lossy schemes provide much higher compression ratio than lossless schemes. Lossy schemes are widely used since the quality of the reconstructed images is adequate for most applications .By this scheme, the decompressed image is not identical to the original image, but reasonably close to it.

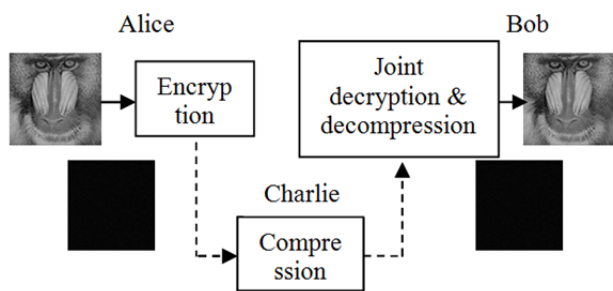


Fig. 1: Encryption-Then-Compression System

## 2. WAVELET

A mathematical function which cut up data into different frequency components, and then study each component with a resolution matched to its scale is known as Wavelet. In analyzing physical situations where the signal contains discontinuities and sharp spikes. Wavelet method has many advantages over the traditional Fourier methods. These are the functions which satisfy certain mathematical requirements and are used in representing data or other functions. This idea is not new; since the early 1800's, approximation using superposition of functions has existed when Joseph Fourier discovered that he could superpose sines and cosines to represent other functions. However, in wavelet analysis, the scale that we use to look at data plays a special role. At a determination interpreted information can then be sorted which matches its scale. The procedure of wavelet analysis is to adopt a wavelet prototype function, known as an analyzing wavelet or mother wavelet. There are two types of analysis i.e. temporal analysis and frequency analysis. Temporal analysis is performed with a contracted, high-frequency version of the

prototype wavelet, whereas frequency analysis is performed with a dilated, low-frequency version of the same wavelet.

### 2.1 Discrete Haar Wavelet Transform (DHWT)

An outstanding property of the Haar functions is that except function Haar (0, t), the  $i^{th}$  Haar function can be generated by the restriction of the  $(j - 1)^{th}$  function to be half of the interval where it is different from zero, by multiplication with  $\sqrt{2}$  and scaling over the interval [0, 1]. These properties give considerable interest of the Haar function, since they closely relate them to the wavelet theory. In this setting, the first two Haar functions are called the global functions, while all the others are denoted as the local functions. Hence, the Haar function, which is an odd rectangular pulse pair, is the simplest and oldest wavelet. The motivation for using the discrete wavelet transform is to obtain information that is more discriminating by providing a different resolution at different parts of the time–frequency plane. The wavelet transforms allow the partitioning of the time-frequency domain into non-uniform tiles in connection with the time–spectral contents of the signal. The wavelet methods are strongly connected with classical basis of the Haar functions; scaling and dilation of a basic wavelet can generate the basis Haar functions.

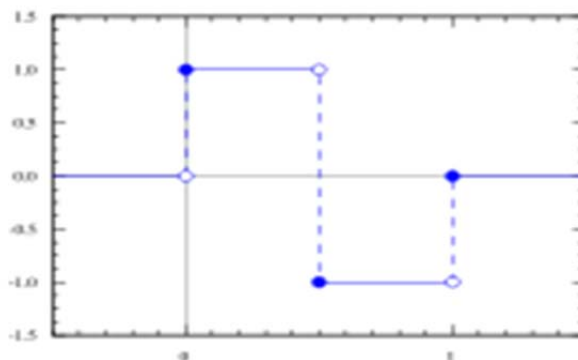


Fig. 2: Haar function on real line [2]

The Haar wavelet operates on data by calculating the sums and differences of adjacent elements. The Haar wavelet operates first on adjacent horizontal elements and then on adjacent vertical elements. Then it operated transformation coding and then encoding steps take place. For the retrieval of original image inverse process needs to follow so that the reconstruction of image can take place.

### 2.2 Coiflet Wavelet

Coiflets are discrete wavelets designed by Ingrid Daubchies, at the request of Ronald Coifman, to have scaling functions with vanishing moments. The wavelet is near symmetric; their wavelet functions have  $N/3$  vanishing moments and scaling

functions  $N/3 - 1$ , and have been used in many applications using Calderón-Zygmund Operators.

Both the scaling function (low-pass filter) and the wavelet function (High-Pass Filter) must be normalized by a factor  $1/\sqrt{2}$ . Below are the coefficients for the scaling functions for C6-30. The wavelet coefficients are derived by reversing the order of the scaling function coefficients and then reversing the sign of every second one (i.e. C6 wavelet =  $\{-0.022140543057, 0.102859456942, 0.544281086116, -1.205718913884, 0.477859456942, 0.102859456942\}$ ). Mathematically, this looks like  $B_k = (-1)^k C_{N-1}$  where  $k$  is the coefficient index;  $B$  is a wavelet coefficient and  $C$  a scaling function coefficient.  $N$  is the wavelet index, i.e. 6 for C6. A biorthogonal wavelet is a wavelet where the associated wavelet transform is invertible but not necessarily orthogonal. Designing biorthogonal wavelets allows more degrees of freedom than orthogonal wavelets. One additional degree of freedom is the possibility to construct symmetric wavelet functions. In the biorthogonal case, there are two scaling

functions  $\phi, \tilde{\phi}$ , which may generate different multi resolution analyses, and accordingly two different wavelet functions  $\psi, \tilde{\psi}$ . So the numbers  $M$  and  $N$  of coefficients in the scaling sequences  $a, \tilde{a}$  may differ. The scaling sequences must satisfy the following biorthogonality condition

$$\sum_{n \in \mathbb{Z}} a_n \tilde{a}_{n+2m} = 2 \cdot \delta_{m,0}$$

Then the wavelet sequences can be determined as

$$b_n = (-1)^n \tilde{a}_{M-1-n} \quad (n = 0, \dots, N-1)$$

$$\tilde{b}_n = (-1)^n a_{M-1-n} \quad (n = 0, \dots, N-1)$$

In *coif*  $N$ ,  $N$  is the order.

Coiflet wavelets are discrete wavelet outlined by Ingrid Daubchies, on the requisition of Ronald Coifman, to have scaling operations with vanishing time period. The wavelet is closing symmetric and their wavelet operation has  $N/3$  vanishing time period and the scaling operation is  $N/3-1$ . They have been utilized in numerous applications by the use of Calderón-Zygmund Operators. Both the scaling operation and the wavelet operation must be normalized by a consideration  $1/\sqrt{2}$ . The following are the coefficients for the scaling operations for C6-30. The wavelet coefficients are demonstrate by switching the request of the scaling capacity coefficients and after that turning around the indication of each second one (i.e. C6 wavelet =  $\{-0.022140543057, 0.102859456942, 0.544281086116, -1.205718913884, 0.477859456942, 0.102859456942\}$ ).

Scientifically, where  $k$  is the coefficient file and  $B$  is a wavelet coefficient and  $C$  a scaling capacity coefficient and  $N$  is the wavelet.

## 2.3 Symlet Wavelet

Symlet wavelets are a family of wavelets. They are a modified version of Daubchies wavelets with increased symmetry. In *sym*  $N$ ,  $N$  is the order. Some authors use  $2N$  instead of  $N$ . Symlets are only near symmetric; consequently some authors do not call them symlets. More about symlets can be found in [Dau92], pages 194, 254-257. By typing `wave info('sym')` at the MATLAB command prompt, you can obtain a survey of the main properties of this family [11].

## 2.4 Daubchies

Daubchies proposes modifications of her wavelets that increase their symmetry can be increased while retaining great simplicity.

The idea consists of reusing the function  $m_0$  introduced in the *db*  $N$ , considering the  $|m_0(\omega)|^2$  as a function  $W$  of  $z = e^{i\omega}$ .

Then we can factor  $W$  in several different ways in the form  $W(z) = U(z)\overline{U(\frac{1}{z})}$  because the roots of  $W$  with modulus not equal to 1 go in pairs. If one of the root is  $z_1$ , then  $\frac{1}{z_1}$  is also a root.

- By selecting  $U$  such that the modulus of all its roots is strictly less than 1, we build Daubchies wavelets *db*  $N$ . The  $U$  filter is a "minimum phase filter."
- By making another choice, we obtain more symmetrical filters; these are symlets.

The symlets have other properties similar to those of the *db*  $N$ s.

## 3. ARITHMETIC CODING

It is most often used when we have to code binary symbols or bits. Each bit begins the coding process. The arithmetic codes generate non-block codes; that is a correspondence between source symbols and code words does not exist. Instead, an entire sequence of source bits is allocated to a single code word which defines an interval of real numbers between 0 and 1.

As the number of symbols or bits in the message increases, the interval used to represent it becomes smaller and the number of bits needed to represent the interval becomes larger. Each symbol in the message reduces the size of the interval according to its probability of occurrence. Since the symbols are not coded one at a time, this technique can achieve the highest possible coding efficiency.

#### 4. METHODOLOGY

##### Encryption-Compression using New Haar, Coiflet, Symlet and Daubchies wavelet transform (ECNHCSNDWT)

The input image has been considered as ‘I’, encryption over ‘I’ has been implemented using random permutation method. The obtained result after encryption has been considered as ‘I<sub>e</sub>’, and then a new Haar, Coiflet, Symlet and Daubchies wavelet technique has been used for compression. The output after compression has been stored as image ‘B’. Then the image ‘B’ has been decrypted after decompression. [1]

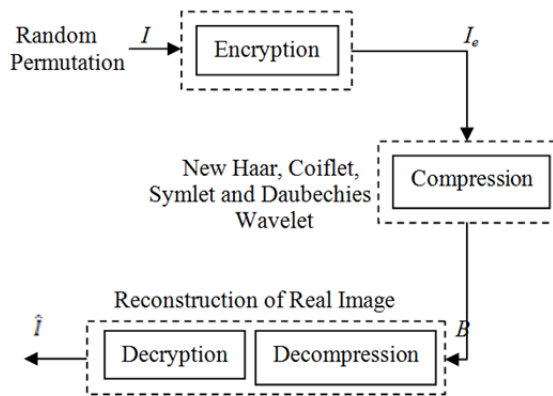


Fig. 3: Proposed Model for Encryption-Compression System

As shown in Fig. 3. Encryption-Compression system is proposed. The resultant image  $\hat{I}$  is evaluated using various parameters like CR, MSE and PSNR to check the efficiency and to compare it with the result of existing system. We can also represent the proposed schema with the help of flowchart. Fig.4. Shows the flowchart that represents the procedure flow of various steps. Half of the flowchart represents the encryption steps and rest represents the compression steps. Then inverse process to retrieve the real image and then calculation steps to check the efficiency.

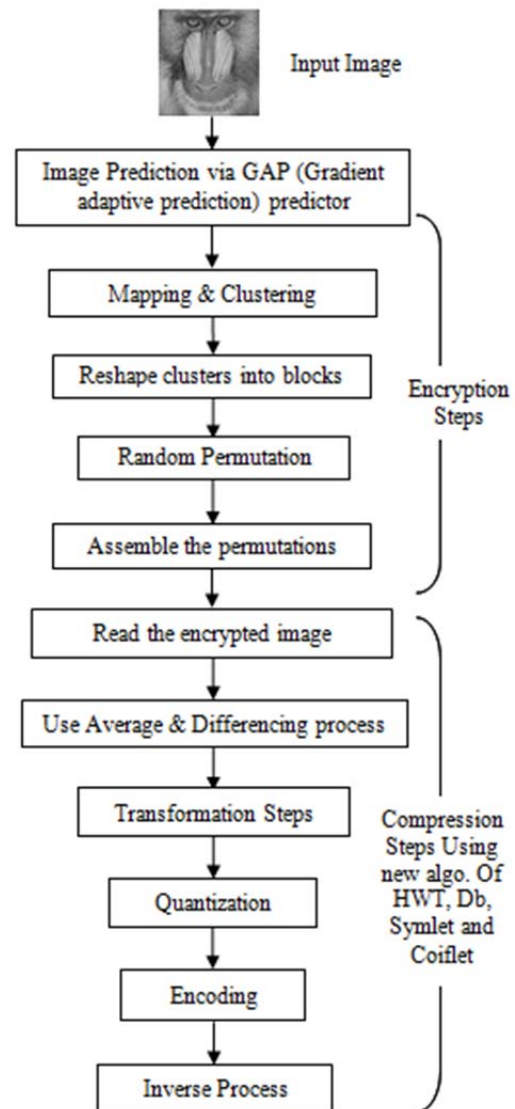


Fig. 4: Flowchart for Image Encryption-Compression Scheme

### 5. EXPERIMENTAL RESULTS

In this section, we perform experiments to verify the efficiency of our approach. The comparison of the accuracy is done for every method is one with the given values to the proposed work. The accuracy rate is much higher in the proposed work as compare to the previous working methods.

#### CR, MSE & PSNR Calculation for Performance Analysis

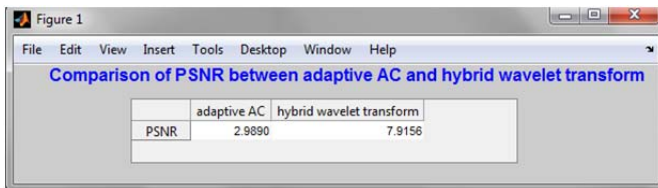
For the performance analysis images of Baboon, Penguins Boat, Peppers and Goldhill are considered as input images. The CR, MSE and PSNR of different input images are shown in table 4.1 and table 4.2 shows the comparison of proposed work with the existing one.

**Table 1: CR, MSE, PSNR for proposed method (ECNHCSNDWT)**

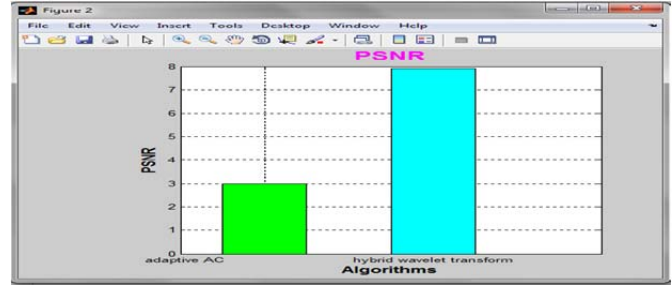
S. No.	Image (.jpeg) (512x512) pixels	CR (Compression Ratio)	MSE (Mean Square Error)	PSNR (Peak Signal to Noise Ratio)
1	Baboon	1.63038	23.8403	51.5365
2	Penguins	1.74454	24.1082	51.4637
3	Boat	1.65273	23.9545	51.5306
4	Peppers	1.47527	21.0726	52.3404
5	Goldhill	1.02743	20.2450	49.9136
<b>Average</b>		1.50607	22.64412	51.35696

**Table 2: Comparison of PSNR for Existing method (ETC) & proposed method (ECNHCSNDWT)**

S. No.	Image (.jpeg) (512x512) Pixels	PSNR of ETC System [1] (Existing method)	PSNR of ECNHCSNDWT System (Proposed method)
1	Baboon	49.91	51.54
2	Penguins	49.89	51.46
3	Boat	49.90	51.53
4	Peppers	49.89	52.34
5	Goldhill	49.89	49.91
<b>Average</b>		49.89	51.35



**Fig. 5: Comparison of PSNR between adaptive AC and hybrid wavelet transform.**



**Fig. 6: Graphical representation of comparison between adaptive AC and hybrid wavelet transform**

### 6. CONCLUSION

In this research work, we have designed an efficient image Encryption-Compression system. Within the proposed framework, the image encryption has been achieved via random permutation. Highly efficient compression of encrypted image has been realized by a new image compression algorithm of Haar, Symlet, Coiflet and Daubchies wavelet transform. Experimental results have shown that reasonably high level of security has been retained. More notably, the coding efficiency of our proposed compression method on encrypted images is very close to that of state-of-art Lossy image codecs, which receive original, unencrypted images as input. The PSNR values for resultant images are better than the previous one. Better PSNR indicates that the reconstruction of image is of higher quality.

### 7. FUTURE WORK

In future the same technique can be extended by applying different transforms to cover image and thus robustness of algorithm can be verified. Following points can be considered in future research work:-

**Data Set:** The data set is limited to the images. As the research is not only related to the encryption and compression of the images, the analysis and comparison of the compression ratio and security is also a part of the research. It can be increased according to application area.

**Parameters and Techniques:** Different parameters for defining the better compression rate and security measures can be consider in future. Different techniques can be used to check the accuracy of the result. Thus in future the work can be done for specific area or specific application, by using different images.

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